

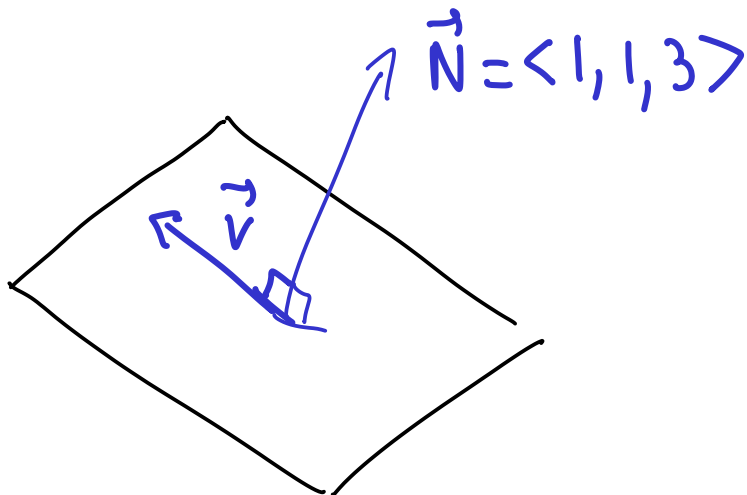
The vector  $\vec{v} = \langle 1, 2, -1 \rangle$  and the plane  $x + y + 3z = 5$  are

① parallel

~~② perpendicular~~

~~③ neither~~

$\vec{v}$  not  $\parallel \vec{N}$

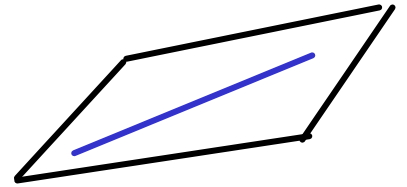


$$\begin{aligned}\vec{v} \cdot \vec{N} &= \langle 1, 2, -1 \rangle \cdot \langle 1, 1, 3 \rangle \\ &= 1 + 2 - 3 = 0\end{aligned}$$

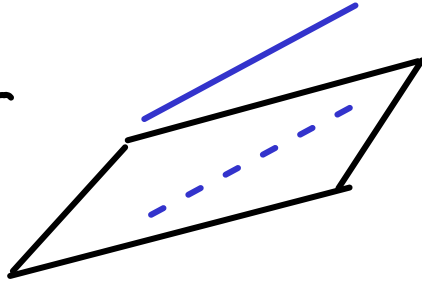
$$\vec{v} \perp \vec{N}$$

## A LINE AND A PLANE:

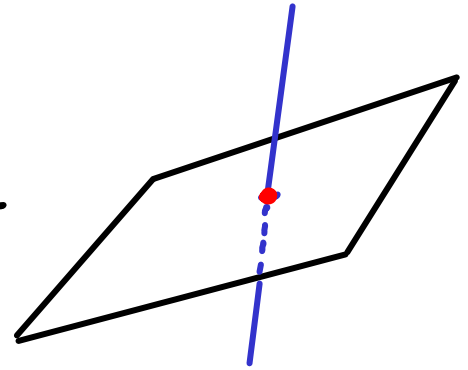
→ The line can be contained in the plane



→ or parallel to it



→ or intersects the plane in a point



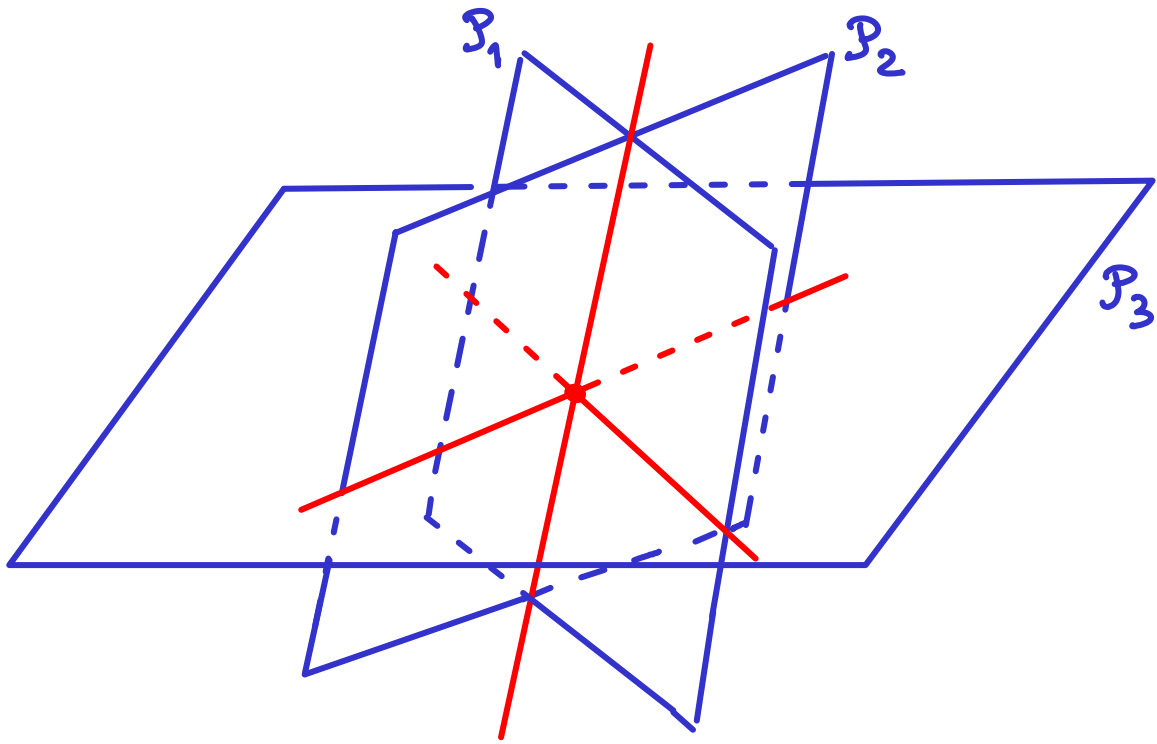
This has to do with:  $3 \times 3$  linear systems!

$$\begin{cases} x + y + 2z = 7 & (P_1) \\ 2x + y - z = 4 & (P_2) \\ x + 2y + 3z = 3 & (P_3) \end{cases}$$

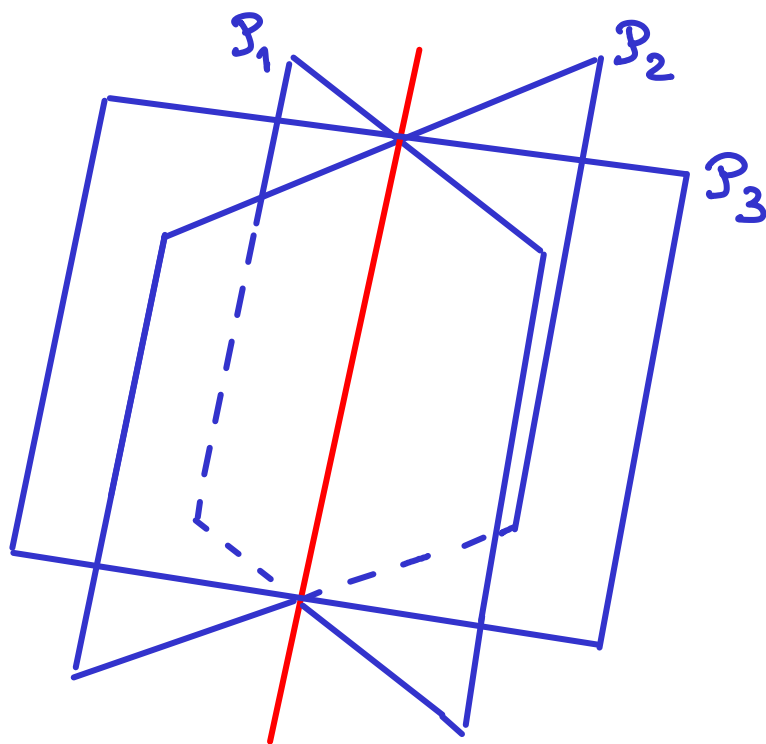
3 planes: where do they intersect?

How many solutions?

If the first 2 planes are not parallel, they intersect in a line.



Line and  $P_3$   
intersect in a point  
(1 solution)

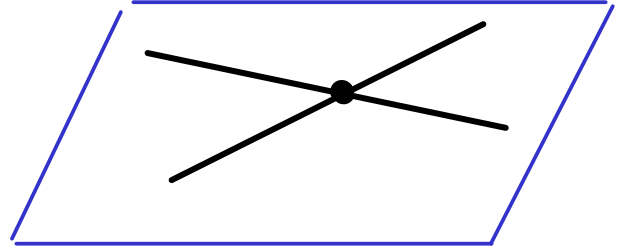
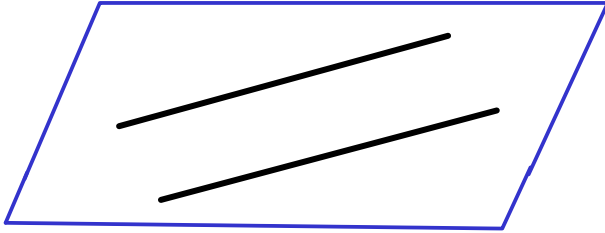


Line  $\parallel P_3$   
(no solution)

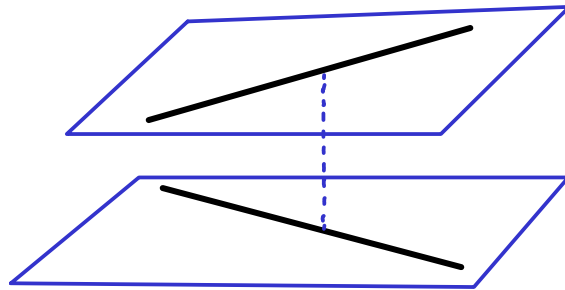
Line contained in  $P_3$   
( $\infty$  solutions)

## RELATIVE POSITIONS OF 2 LINES:

→ parallel } in both cases, a unique plane  
→ intersecting } containing both lines



→ skew lines = neither parallel nor intersecting  
Then they lie on parallel planes



Distance between the 2 planes = shortest distance  
between points on the skew lines.

# CYCLOID

$$\vec{OC} = \langle a\theta, a \rangle$$

$$\vec{CP} = \langle -a \sin \theta, -a \cos \theta \rangle$$

$$\vec{r}(\theta) = \vec{OP} = \vec{OC} + \vec{CP} = \langle a\theta - a \sin \theta, a - a \cos \theta \rangle$$

